Math 170 Problem of the Week for Week 5

Solve for x,

$$\sqrt{1 + \sqrt{1 + x}} = \sqrt[3]{x}$$

(I will put a hint on a separate link. This will be a link to a strategy)

The method I used, towards the end, involves the rational zero test and synthetic/long division

Raise both sides of the equation to the 6th power, since square roots are powers to the one-half and cube roots are powers to the one-third.

Let $u = \sqrt{1 + x}$ and methodically get everything in terms of u.